

# Conversion between continuous-time and discrete-time signals

## Continuous-to-discrete transformation

Consider a bandlimited continuous-time signal  $x_c(t)$ : that is, it has no frequency content for  $|\omega| \geq \omega_c$ .

This signal can be converted to a discrete-time (DT) signal  $x_d[n]$  by sampling  $x_c(t)$  at intervals of  $T$  seconds. This operation is known as continuous-to-discrete (C/D) transformation. In other words,

$$x_d[n] = x_c(nT)$$

The following relations come from this sampling:

$$n = \frac{t}{T}$$

- DT sample count is CT time divided by the sampling period.

$$\Omega = \omega T$$

- DT frequency is CT frequency multiplied by the sampling period.

**Nyquist's sampling theorem** states: if the sampling frequency is greater than twice the highest frequency in a signal ( $\omega_c$  in this example), then we can reconstruct the CT Fourier transform of a signal, and thus also the CT signal, from the DT Fourier transform of the sampled DT signal.

The **Nyquist rate** is twice the highest frequency in a signal. The sampling rate should be at least this value to avoid aliasing. This condition can also be written as:

$$f_s = \frac{1}{T} \geq \frac{\omega_c}{\pi} = 2f_c$$

If this condition is met, then:

$$X_d(e^{j\Omega}) = \frac{X_c(j\omega)}{T}$$

- The DT Fourier transform is equal to the CT Fourier transform divided by the sampling period.

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Last update: 2024-04-30 04:03

